# Class Size And Student Achievement: A Parametric Paired $T$-Test 

Nickanor A. Owuor*<br>Department of Business and Management, University of Kurdistan Hewler, Kurdistan Region - F.R. Iraq<br>*Corresponding author's email: n.amwata@ukh.edu.krd

Received: 05 February 2018
Accepted: 07 June 2018
Available online: 30 June 2018


#### Abstract

The change from elite to mass higher education has arguably heightened pressure on HE in many countries. Therefore, the relevance of class size with regard to student achievement and quality assurance has become such a topical issue. Thus, this study employs a quantitative method by way of a parametric paired $t$-test to investigate the effect of splitting a large class into smaller groups in two successive semesters at an anonymous university. The identity of the university has not been revealed as per prior arrangement with the administration. The data on the students' performance in the two semesters are analyzed, and it is established that there is a positive relationship between class size and student achievement, even though it does not establish specifically how small is best. The paper begins with an introduction, discusses the methodology, then delves into the data, and finally ends with some discussion and conclusion.


Keywords: Class Size, Higher Education, Paired $t$-test, Student Achievement, University

## 1. INTRODUCTION

There is undoubtedly prolific research and debate as to whether a large class size may have any bearing on student achievement, There is undoubtedly prolific research and debate as to whether a large class size may have any bearing on student achievement. This applies to schools, e.g., (Blatchford, 2003) or even in higher education. Some of these studies indicate a negative effect of class size on student performance and satisfaction according to the studies of Kokkelenber et al., 2008, and Mandel and Sussmuth, 2011, while according to the studies of Chapman and Ludlow (2010), Johnson (2010), and McDonald (2013), other studies such as the arguments by Biggs (1998), Ceci and Konstantopoulos (2009), and Rotherham (2011) do not indicate an indifference.

| Access this article online |  |
| :--- | :--- |
| DOI: $10.25079 /$ ukhjss.v2n1y2018.19-24 | E-ISSN: 2520-7806 |

Copyright © 2018 Nickanor A. Owuor. Open Access journal with Creative Commons Attribution Non-Commercial No Derivatives License 4.0 (CC BY-NC-ND 4.0).

The influence of class size on the university students' performance has long been a subject of interest. While it is generally believed that, in a small class, there is more student-teacher interaction and thus more effective learning than in a large class (Tseng, 2010), Toth and Montagna (2002) in an analysis of literature from various studies on the subject discovered that there were mixed results; some of them indicate a positive relationship while others indicate the contrary.

### 1.1. Institutional Context

In the past few years, the university (whose name shall remain anonymous) has undergone tremendous change. One such fundamental change has been occasioned by the shift from being a specialist, elite higher education provider to a more expanded enrollment with a sort of "open arms" admissions policy. At inception in 2006, the original mission was for the university to act as the Center of Excellence in its region and to offer specialist social science training, an area that had been identified as lacking capacity at the time. So to start with, only four undergraduate programs were launched: in Politics and International Relations, Business and Management Sciences, Sociology, and Computers Applied IT. Besides
this, there was also a compulsory Access Program, a 2-year preparatory program where all the students enrolled were expected to undertake a 2 -year intensive training in English, communication skills, and life skills in general. After the 2-year Access Program, the students would then progress to their respective undergraduate programs. The admission process was also very rigorous, with applicants having to undergo aptitude tests and all that. In the first admission year, only 100 students gained entry out of a large pool of up to 600 or so applicants. They would then be distributed to the four programs. In casual interview with one of the former lecturers, he thusly said: "I had the privilege of teaching some of these students, having been with the university since 2009, and admittedly the quality and caliber of students then was quite remarkable. I believe most of my colleagues had the same opinion on this lot" (Anonymous, Interview, May 10, 2015).

First forward to a few years later, there came a new policy to gradually increase the enrollment. Understandably, this was meant to build a critical mass for the impact of the programs to be felt and also to secure the future of the university. Hence, year by year, the enrollment went up from 100 to 180 and then double to 360 . That is not all, it went up further to 450 and ultimately to 600 currently. The number was considered quite staggering, given that the facilities have not been extended commensurately and we are still based on the same old and small campus that was meant to host fewer students.

Other changes that were effected over the years included the abolition of the Access Program and extended the duration of undergraduate program from 3 to 4 years.

### 1.2. Statement of the Problem

Against the aforementioned backdrop, in the first semester of the academic year 2014-2015, the undergraduate year two students took a module "Principles of Marketing." It was such a "large" class of up to 81 students put together. Throughout the semester, the lecturer reported that he had to contend with a lot of challenges that come with managing such large groups of students, including lack of concentration by students and other behavioral issues. As one would expect, the overall student performance was also not quite satisfactory. Taking cognizance of this, in the second semester, it was resolved within the department to split the class into three groups as a necessary intervention.

This study, therefore, was intended to study the effect of this intervention on the students' overall performance in the second semester.

### 1.3. Research Question

The central question in this research was:

- Is there any relationship between the class size and students' overall academic achievement?
Answering this question was pivotal in proving the case for small class sizes or otherwise.


### 1.4. Hypothesis

If $\mathrm{x}=$ marks in semester one, before the class is split, and $\mathrm{y}=$ marks in semester two, after the class has been split, and the respective means are $\mu_{1}$ and $\mu_{2}$, the relevant hypothesis in this study is:
$\mathrm{H}_{0}=\mu_{1}=\mu_{2}$ (population means are equal, i.e., there is no relationship between class size and class performance).
$\mathrm{H}_{\mathrm{A}}=\mu_{1} \neq \mu_{2}$ (population means are not equal, i.e., there is a relationship between class size and class performance).

### 1.5. Scope and Limitation

A key assumption of this study is that citerisparibus only class size may influence student achievement. Like most empirical research on class size which utilizes outcome measures such as final course grades, standardized test scores, or other course evaluation data (Johnson, 2010), other factors that may also comprise learning achievement are often ignored. However, arguably, like in this instance, course offerings at different intervals may not be exactly the same thus raising concerns as to whether we might be comparing "apples" with "oranges."

### 1.6. Class size: What is Small or large?

This is the question that has perhaps been asked so many times. Hence, what makes an appropriate class size and when would a class be considered too small or too large to be meaningful?

Class size even though often confused with the staff-student ratio (SSR) means quite a different thing and is used to refer to the actual number of learners taught by a teacher at a particular time as compared to SSR which may include even staff with other roles outside the classroom (Ehrenberg et al., 2001).

In some countries or institutions there may be legislation or policy on maximum class size especially in schools. For example, in Norway there is the rule of 30 students (Bonesronning, 2003), whereas in the US it varies from state to state, where for some it is 15 , while others have it at 17 , yet
others at 20 (Ehrenberg, Brewer, Gamoran, \& Willms, 2001). In our university there has not been any policy of sorts and the interventions might as well be considered just ad hoc by the department.

According to Maringe and Sing (2014), there is generally no well-accepted definition of what a typical large class is even though they indicate that most empirical studies in this area tend to put at classes with more than 100 students based on evidence drawn from such classes.

While larger class sizes present economies of scale and opportunity for increased revenues, especially in the light of economic realities in recent years, it is not an easy choice either. Stakeholders such as higher education administrators are faced with a dilemma as to how to maintain and enhance their institutional reputation through small student-to-faculty ratios among rising education costs. Students too are known to consider class size in their choice of university, study programs, and courses (Westerlund, 2008; Bedard and Kuhn, 2008).

## 2. RESEARCH METHODOLOGY

To tackle the research question, the study employed a quantitative design utilizing two data sets, i.e., students' marks in semester one as a large group before the split and the marks in the second semester after the split. The data were then analyzed using the paired $t$-test, a technique usually used when dealing with two samples that are dependent (Rosner, 1982; Yang and Tsiatis, 2001), like in this case, where each instance in one dataset has a unique connection with the other data set. The samples from the data sets are drawn at random. The following formula is used to determine the sample size:
$\mathrm{n}=(\text { Z-score })^{2} * \operatorname{StdDev}^{*}(1-\mathrm{StdDev}) /(\text { margin of error })^{2}$
$=68$

Where:

Margin of error $=5 \%$

Confidence level $=95 \%$
Population size $=81$
The theoretical base in the study revolved around the two dimensions of class size and students' academic achievement.

To accomplish a systematic review of literature, Creswell's (2002) five-step process was applied: "...identifying terms to typically use in your literature search; locating literature; reading and checking the relevance of the literature; organising the literature you have selected; and writing a literature review" (p. 86).

### 2.1. Ethical Issues

The study and all its aspects had to be subjected to strict ethical guidelines and standards. For purposes of confidentiality, the institution has been anonymized instead of using the actual name. The identities of any of the participants have also not been revealed.

## 3. DATA ANALYSIS AND DISCUSSION

Table 1 shows the raw data for the samples and the analysis performed thereon.

### 3.1. Hypothesis Test

The paired $t$-test is used here to compare one set of data(x) with a second $\operatorname{set}(y)$ from the same sample. It is used to compare the "pre" and "post" student scores of splitting the class and to determine whether any change might have occurred.

The formula is presented below.
$t=\frac{\bar{x}-\Delta}{\frac{s}{\sqrt{n}}}$
Where:

- is the mean of the change scores,
$\Delta$ - is the hypothesized difference ( 0 if testing for equal means),
$s$ - is the sample standard deviation of the differences, and
$n$ - is the sample size.
While the degrees of freedom is $n=1$.
Using Microsoft Excel to perform the calculation, the result in Table 2 is derived. The two-tailed test is pictorially presented in Figure 1, indicating that there is a significant difference between the means with probability distribution for a $95 \%$ confidence level.

Table 1: Raw sample data and calculation

| S. No $\quad$ Student No. | $\mathbf{x}=$ marks in semester one before the |
| :--- | :--- | :--- | :--- | :--- |
| class is split |  |$\quad$| $\boldsymbol{y}=$ marks in semester two after the class |
| :---: |
| has been split |$\quad$ Difference


| 1 | 1100432 | 37 | 58 |
| :--- | :--- | :--- | :--- |
| 2 | 1100178 | 42 | 51 |
| 3 | 1100196 | 40 | 62 |


| 4 | 1100376 | 48 | 55 |
| :--- | :--- | :--- | :--- |
| 5 | 1100095 | 70 | 77 |


| 5 | 1100095 | 70 |
| :--- | :--- | :--- |


| 1100166 | 23 | 44 |
| :--- | :--- | :--- | :--- |
| 100079 | 17 | 48 |

8 -
1100288
1100060
1100052
1100212
1100179
1100351
1200198
1000101
1000102
1100379
1100118
1100144
1100091
1100202
1100028
1100064
1100421
1100131
100398
1100398 -
1100208
1100223
1100090
1000165
1000165
1100049
1100404
1100404
1100057
1100207
1200949
1200949
1000018
1200284
1100249
1300019
1100154
1300015
1100415
1100240
1100220
1200697
1100272
1100373
1100071

| 1100438 | 38 | 45 | 7 |
| :---: | :---: | :---: | :---: |
| 1200104 | 15 | 35 | 20 |
| 1201670 | 43 | 56 | 13 |
| 1200917 | 72 | 80 | 8 |
| 1300017 | 70 | 73 | 3 |
| 1300011 | 40 | 45 | 5 |
| 1100098 | 23 | 38 | 15 |
| 1300010 | 60 | 69 | 9 |

Table 1: (Continued)

| S. No | Student No. | $\mathbf{x}=$ marks in semester one before the class is split | $y=m a r k s$ in semester two after the class has been split | Difference |
| :---: | :---: | :---: | :---: | :---: |
| 58 | 1200284 | 18 | 34 | 16 |
| 59 | 1300012 | 72 | 80 | 8 |
| 60 | 1100443 | 42 | 64 | 22 |
| 61 | 1200424 | 18 | 44 | 26 |
| 62 | 1000029 | 40 | 56 | 16 |
| 63 | 1100114 | 43 | 48 | 5 |
| 64 | 1100369 | 57 | 67 | 10 |
| 65 | 1100068 | 27 | 45 | 18 |
| 66 | 1100103 | 85 | 92 | 7 |
| 67 | 1100296 | 55 | 65 | 10 |
| 68 | 1100340 | 43 | 56 | 13 |
|  | Mean | 44.17647059 | 54.58823529 | 10.4118 |
|  |  |  | Standard deviation | 7.33879 |
|  |  |  | Standard error of difference | 0.88996 |
|  |  |  | T-alpha half at $95 \%$ confidence interval | 1.996008 |
|  |  |  | Lower confidence level | 8.635401 |
|  |  |  | Upper confidence level | 12.18813 |

Table 2: $t$-test: paired two sample for means

| Statistical measures | x=Marks in semester one before the class is split | $y=M a r k s$ in semester two after the class has been split |
| :---: | :---: | :---: |
| Mean | 44.17647059 | 54.58823529 |
| Variance | 359.7594381 | 252.0368745 |
| Observations | 68 | 68 |
| Pearson correlation | 0.926441983 |  |
| Hypothesized mean difference | 0 |  |
| Df | 67 |  |
| $t$ Stat | -11.69915831 |  |
| $\mathrm{P}(\mathrm{T} \leq \mathrm{t})$ one-tail | 3.80095E-18 |  |
| $t$ critical one-tail | 1.667916114 |  |
| $\mathrm{P}(\mathrm{T} \leq \mathrm{t})$ two-tail | 7.60191E-18 |  |
| t critical two-tail | 1.996008354 |  |



Figure 1. $t$ distribution

A negative sign $t$ stat $(-11.699)$ implies that the sample mean is less than the hypothesized mean. This presents a compelling evidence against the null hypothesis.

It, therefore, affirms the alternative hypothesis that there is indeed a relationship between class size and student achievement.

## CONCLUSION

Evidently, from this study, it can be derived that there is a positive relationship between class size and student achievement. Therefore, the contention that class size has no relation with student achievement (Ceci and Konstantopoulos, 2009; Rotherham, 2011) is debunked. However, one key assumption of this study is that citeris paribus only class size may influence student achievement. Practically, there may be several factors that may also come into play inter alia student motivation, learning facilities, teacher's competency, subject complexity, and so on. These have not been considered or explored in this instance. At the same time, the study only serves to establish the efficacy of small size classes but does not establish how small is best. As author Gladwell (2013) puts it, there is definitely a point below which being small may
not produce any better outcomes but may instead produce even worse outcomes.

## REFERENCES

Bedard, K., \& Kuhn, P. (2008). Where class size really matters: Class size and student ratings of instructor effectiveness. Economics of Education Review, 27, 253-265.
Biggs, J. (1998). Learning from the Confucian heritage: So size doesn't matter? International Journal of Educational Research, 29(8), 723-738.
Blatchford, P. (2003). Class Size Debate: Is Small Better? Berkshire: McGraw-Hill Professional Publishing.
Bonesronning, H. (2003). Class size effects on student achievement in Norway: Patterns and explanations. Southern Economic Journal, 69(4), 952-965.
Borland, M. V., Howsen, R. M., \& Trawick, M. W. (2005). An investigation of the effect of class size on student academic achievement. Education Economics, 13(1), 73-83.
Chapman, L., \& Ludlow, L. (2010). Can downsizing college class sizes augment student outcomes? An investigation of the effects of class size on student learning. The Journal of General Education, 59(2), 105-123.
Ceci, S. J., \& Konstantopoulos, S. (2009). It's not all about class size. Chronicle of Higher Education, 55(21), A30.
Ehrenberg, R. G., Brewer, D. J., Gamoran, A., \& Willms, J. D. (2001). Class size and student achievement. Psychological Science in the Public Interest, 2(1), 1-30.
Gladwell, M. (2013). David and Goliath: Underdogs, Misfits, and the Art of Battling Giants. New York: Little, Brown and Company.
Johnson, I. Y. (2010). Class size and student performance at a public research university: A Cross-classified model. Research in Higher

Education, 51(8), 701-723.
Kokkelenber, E. C., Dillon, M., \& Christy, S. M. (2008). The effects of class size on student grades at a public university. Economics of Education Review, 27(2), 221-233.
Mandel, P., \& Sussmuth, B. (2011). Size matters: The relevance and Hicksian surplus of preferred college class size. Economics of Education Review, 30(5), 1073-1084.
Maringe, F., \& Sing, N. (2014). Teaching large classes in an increasingly internationalising higher education environment: pedagogical, quality and equity issues. Higher Education: The International Journal of Higher Education and Educational Planning, 67(6), 761-782.
Mcdonald, G. (2013). Does size matter? The impact of student-staff ratios. Journal of Higher Education Policy and Management, 35(6), 652-667.
Rosner, B. (1982). A generalization of the paired t-test. Applied Statistics, 31(1), 9-13.
Rotherham, A.J. (2011). When it comes to class size, smaller isn't always better. Time, 03 March. Available from: http://www.content.time. com/time/nation/article/0,8599,2056571,00.html. [Last accessed on 2015 May 28].
Toth, L. S., \& Montagna, L. G. (2002). Class size and achievement in higher education: A summary of current research. College Student Journal, 36(2), 253-261.
Tseng, H. (2010). Has the student performance in managerial economics been affected by the class size of principles of microeconomics? Journal of Economics and Economic Education Research, 11(3), 15-27.
Westerlund, J. (2008). Class size and student evaluations in Sweden. Education Economics, 16(1), 19-28.
Yang, L., \& Tsiatis, A. A. (2001). Efficiency study of estimators for a treatment effect in a pretest-posttest trial. The American Statistician, 55(4), 314-321.

